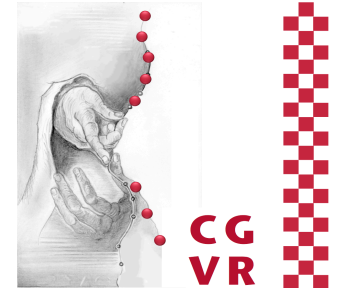


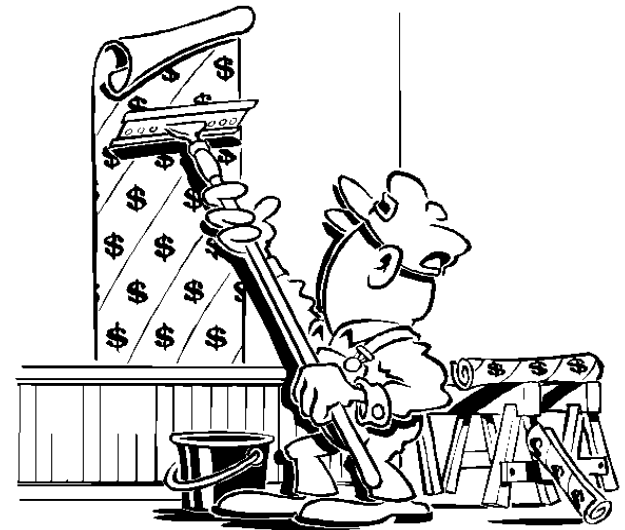
Bremen



Advanced Computer Graphics

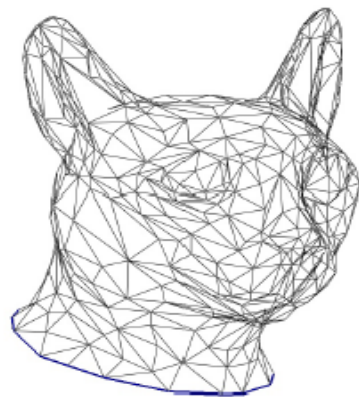
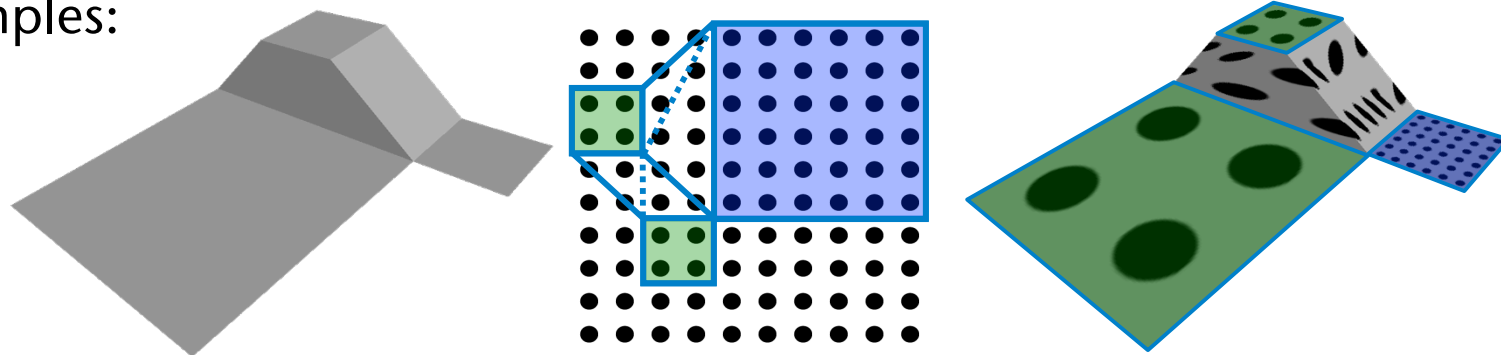
Advanced Texturing Methods

G. Zachmann
University of Bremen, Germany
cgvr.informatik.uni-bremen.de

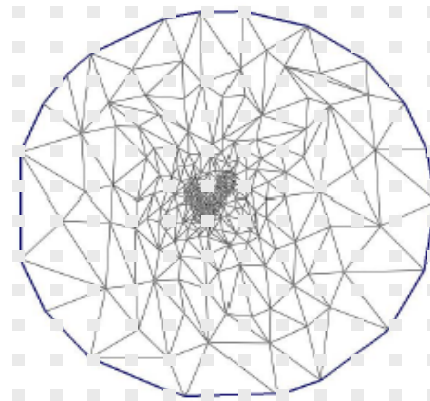


Problems with (Simple) Parameterizations

- Distortions in size & form
- Consequence: **relative over-** or **under-sampling**
- Examples:



Mesh



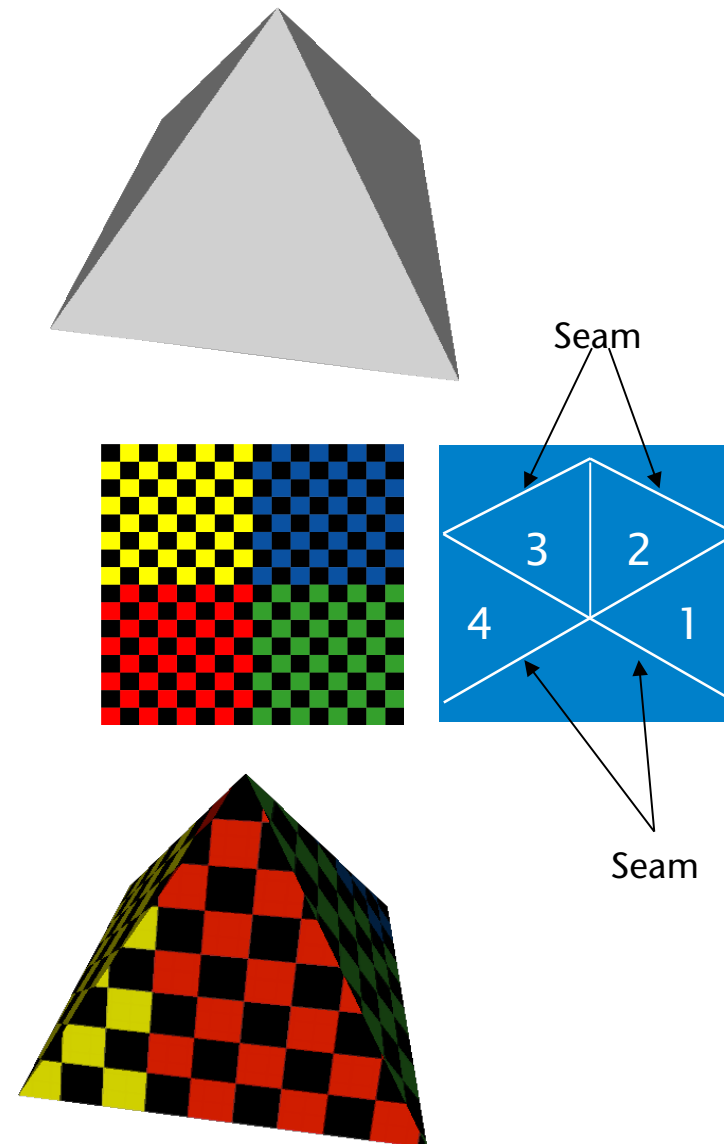
Embedding



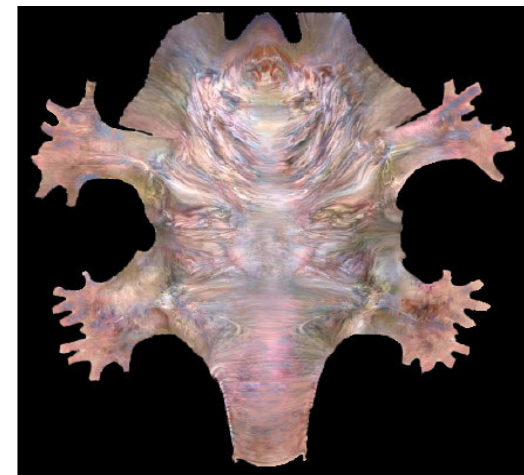
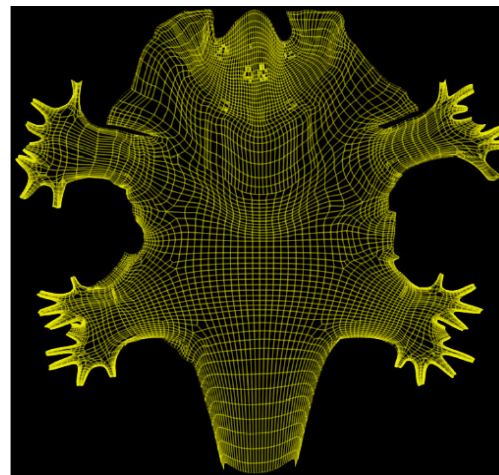
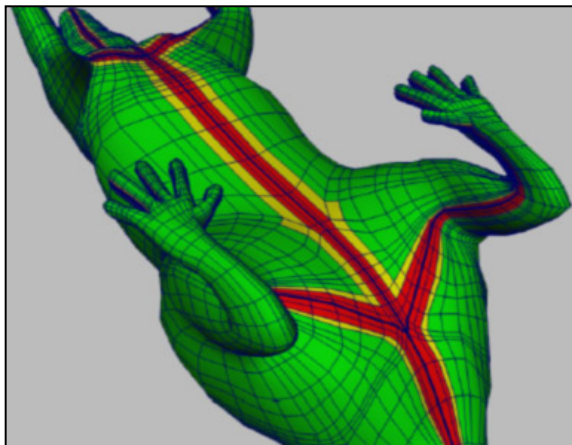
Distortion

One Technique: Seams ("Nähte", Textursprünge)

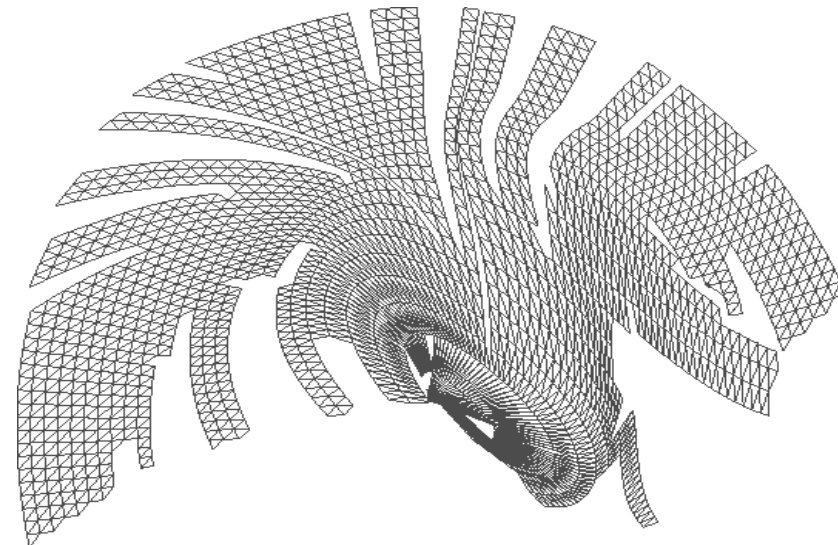
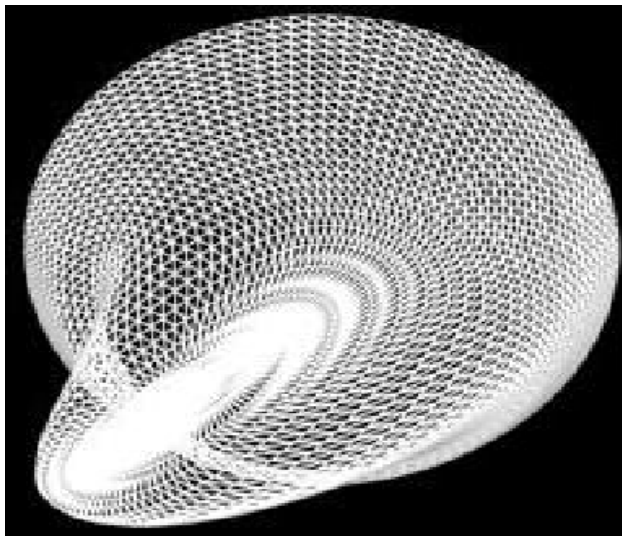
- Goal: minimize the distortion
- Idea: cutting up the mesh along certain edges
- Results in "double edges", also called *seams*
- Unavoidable with non-planar topology



- Cut the object along only **one** continuous edge (preferably at inconspicuous places)
- Effect: the resulting mesh is now topologically equivalent to a disc
- Then embed this cut-open mesh into the 2D plane

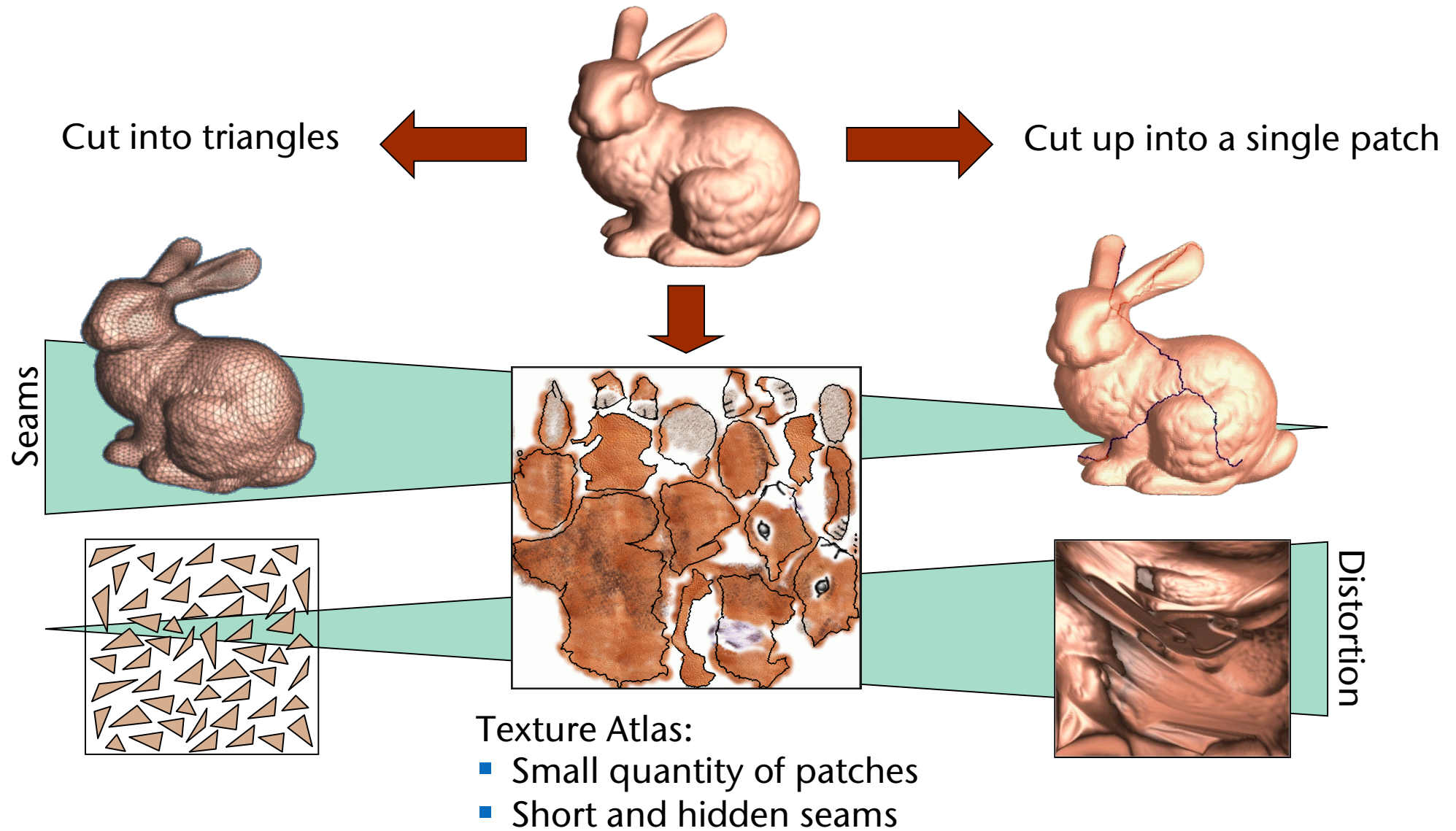


- Problem: there are still distortions
- Straight-forward remedy: multiple incisions
 - Problem: produces a severely fragmented embedded grid with many seams



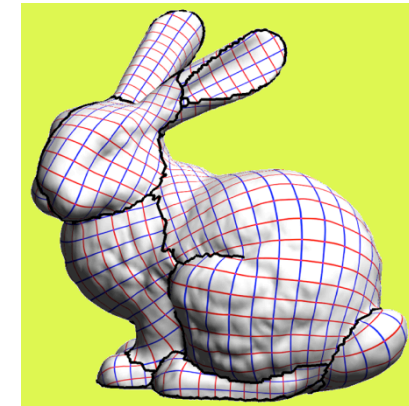
- Another problem with seams: vertices on the seam must have multiple (u,v) coordinates
- Remedy: create multiple copies of those vertices
- New problem in case of deformations of the mesh

Distortion or Seams?

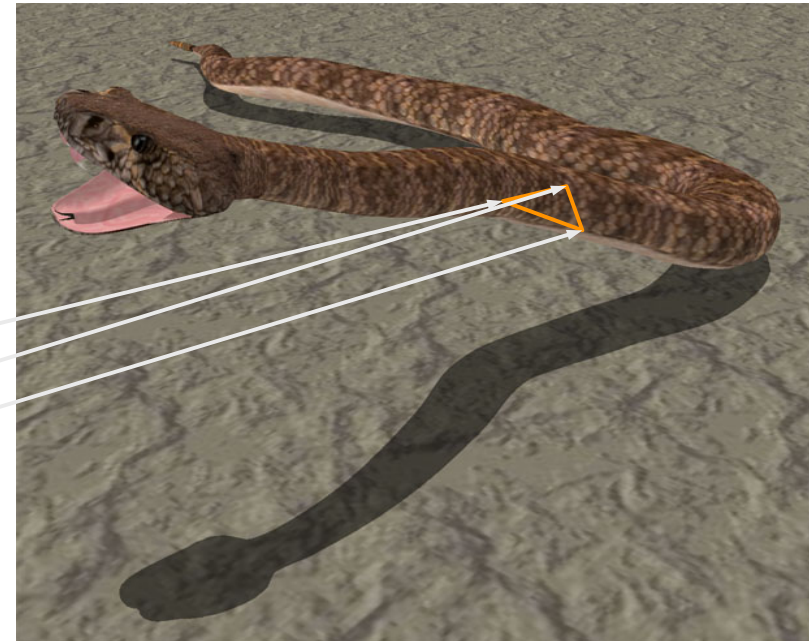
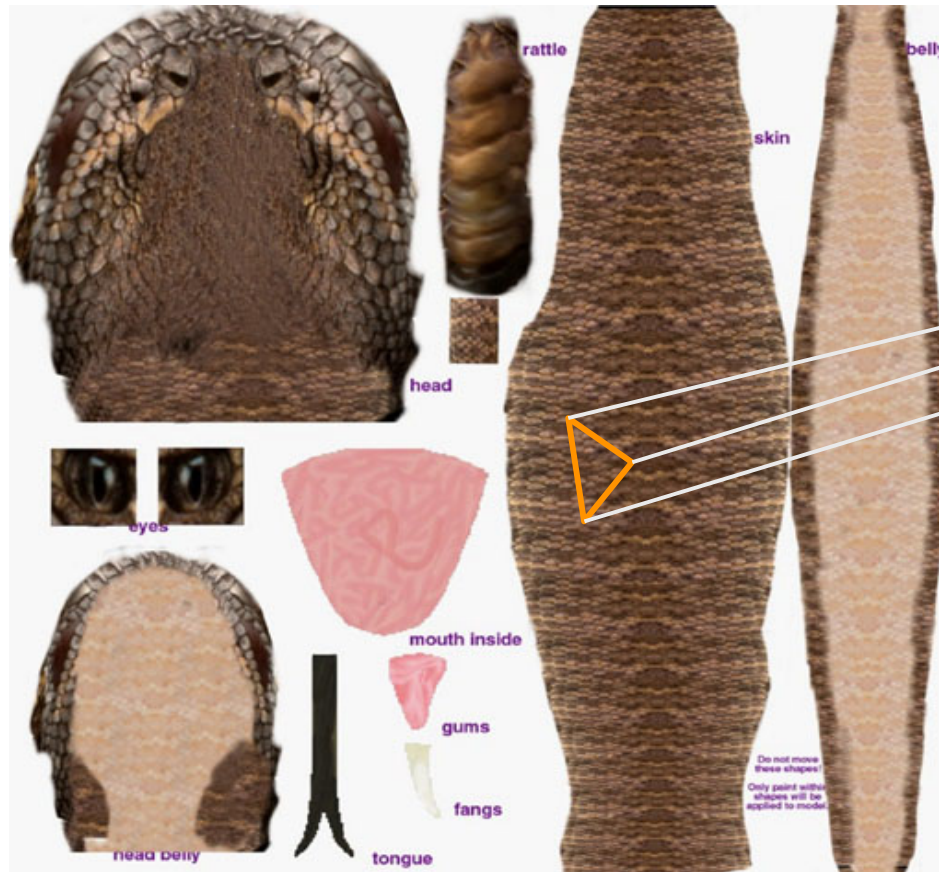


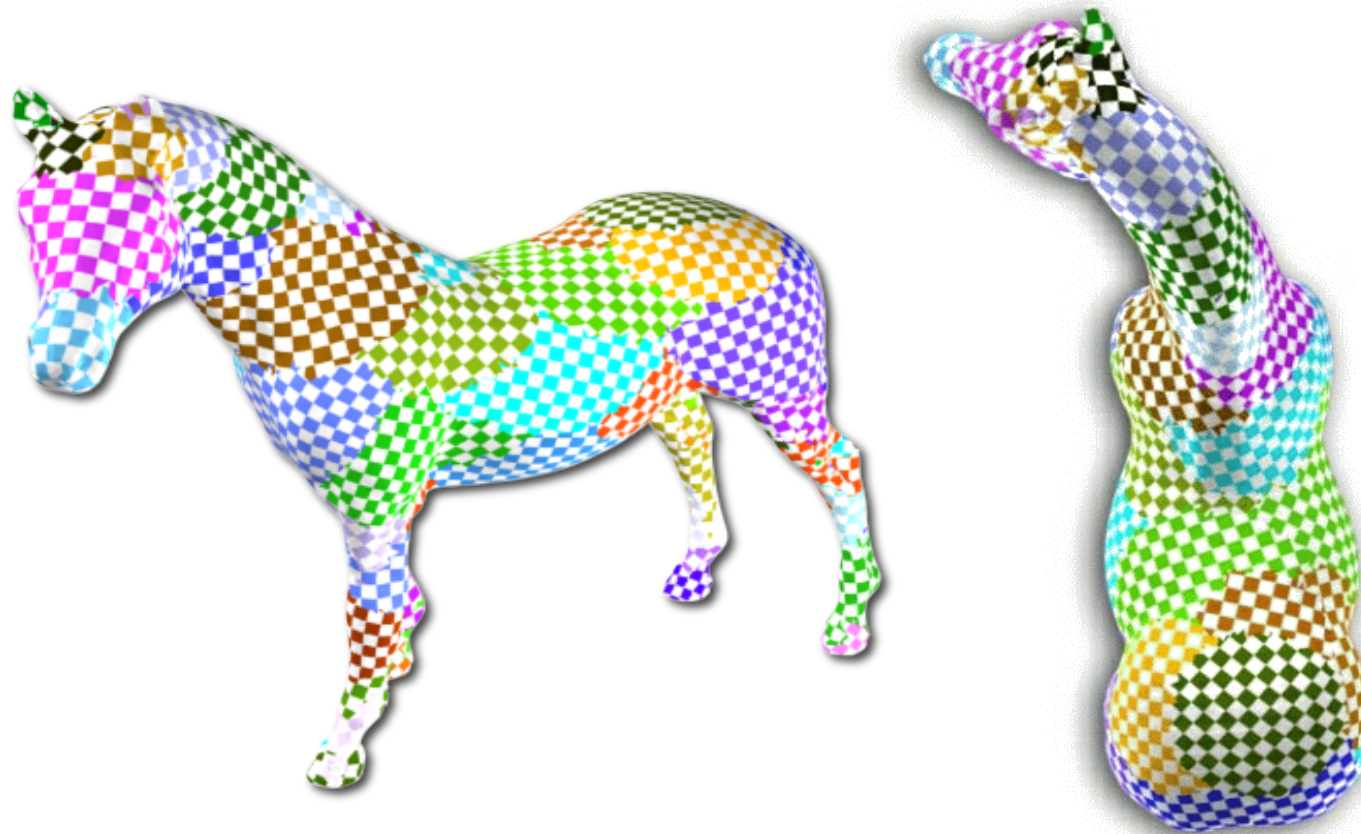
Texture Atlas

- Idea:
 - Cut the 3D surface in individual **patches**
 - **Map** = individual parameter domain in texture space for a single patch
 - **Texture Atlas** = set of these patches with their respective maps (= parameter domains)
- Statement of the problem:
 - Choose a compromise between seams and distortion
 - Hide the cuts in less visible areas
 - How do you do that automatically?
 - Determine a compact arrangement of texture patches (a so-called *packing problem*)



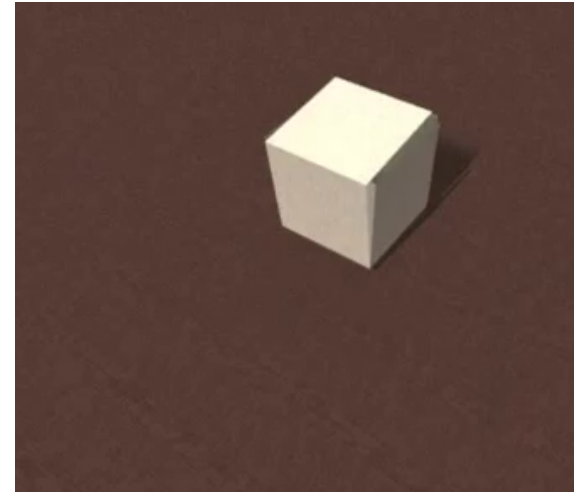
- Example:





Digression: A Geometric Brain-Teaser

- A cube can be **unfolded** into a cross:



Katie Park / unfoldit.org

- Into what other forms can a cube be unfolded, too?



Katie Park / unfoldit.org

- Side note: the (unfolded) cube can be folded into a parallelogram



- BTW: all platonic solids except for the dodecahedron can be folded into a parallelogram in this way ...

Cube Maps

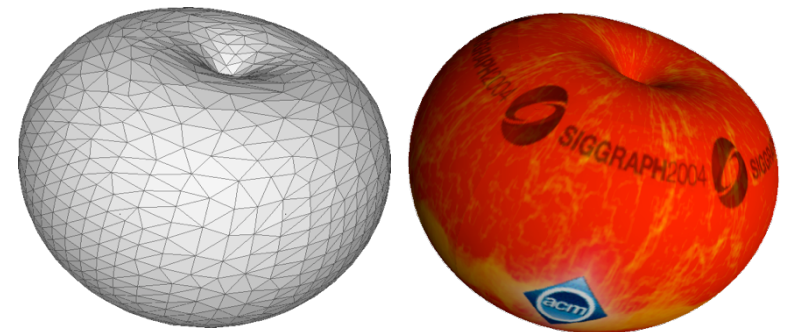
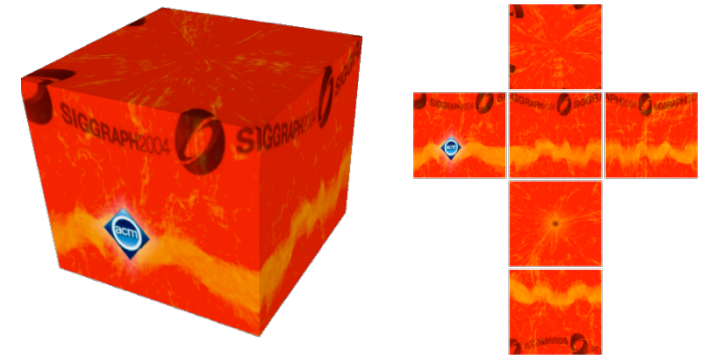
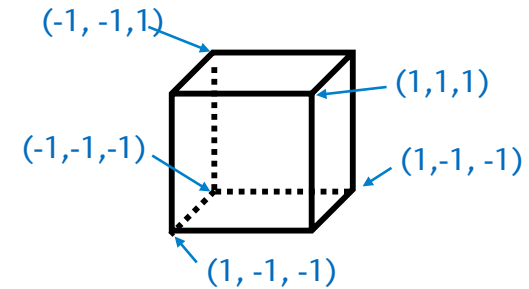
[Greene '86, Voorhies '94]



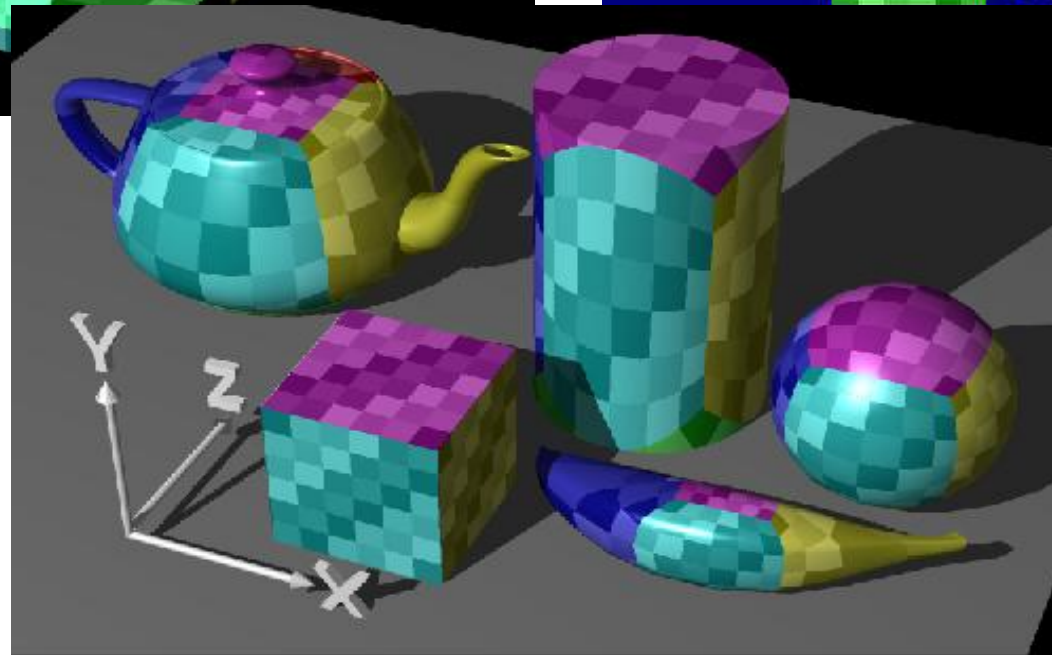
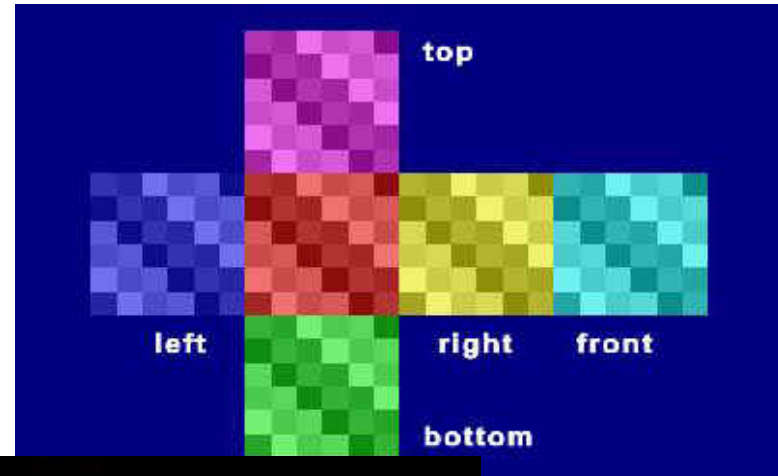
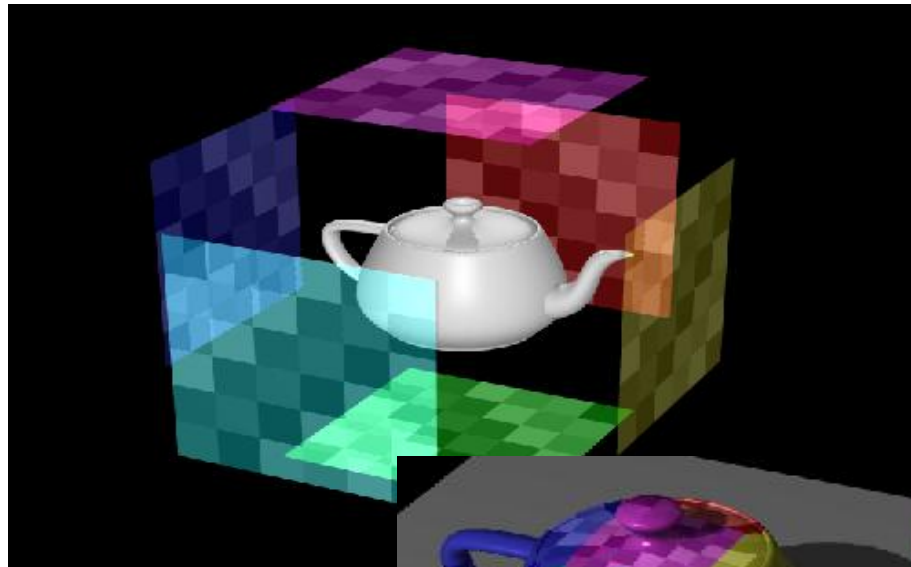
- Parameter domain $\Omega =$ unit cube:
 - Six quadratic texture bitmaps
 - 3D texture coordinates in OpenGL:

```
glTexCoord3f( s, t, r );
glVertex3f( x, y, z );
```

- Largest component of (s,t,r) determines the map, intersection point determines (u,v) within the map
- Rasterization of cube maps:
 1. Interpolation of (s,t,r) in 3D
 2. Projection onto the cube $\rightarrow (u,v)$
 3. Texture look-up in 2D
- Pro: relatively uniform, OpenGL support
- Slight con: one needs 6 images



Examples



```
glGenTextures( 1, &textureID );
glBindTexture( GL_TEXTURE_CUBE_MAP, textureID );
glTexImage2D( GL_TEXTURE_CUBE_MAP_POSITIVE_X, 0, GL_RGBA8, width, height,
              0, GL_RGB, GL_UNSIGNED_BYTE, pixels_face0 );
```

... Load the texture of the other cube faces

```
glTexParameteri( GL_TEXTURE_CUBE_MAP,
                  GL_TEXTURE_WRAP_S, GL_CLAMP_TO_EDGE );
```

... Set more texture parameters, like filtering

```
glEnable( GL_TEXTURE_CUBE_MAP );
glBindTexture( GL_TEXTURE_CUBE_MAP, textureID );
```

```
glBegin( GL_... );
```

```
glTexCoord3f( s, t, r );
```

```
glVertex3f( ... );
```

...

Analog:

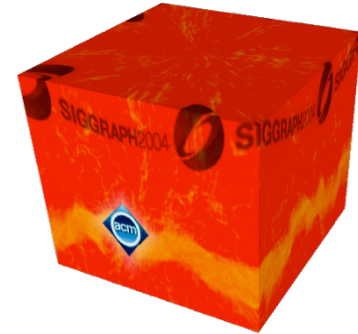
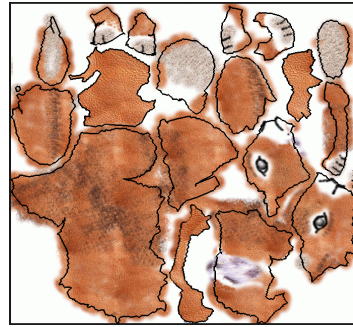
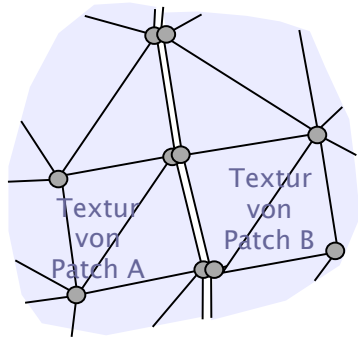
```
GL_TEXTURE_MAG_FILTER,
GL_TEXTURE_WRAP_T, etc. ...
```

Just like with all other vertex attributes in OpenGL:
first send all attributes, then the coordinates

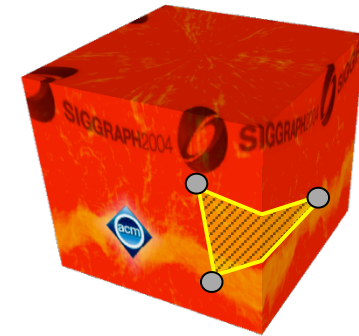
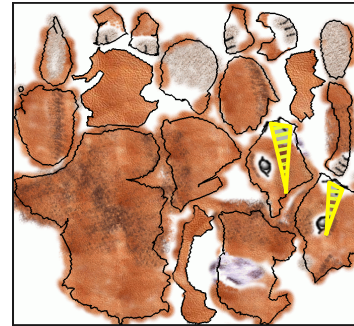
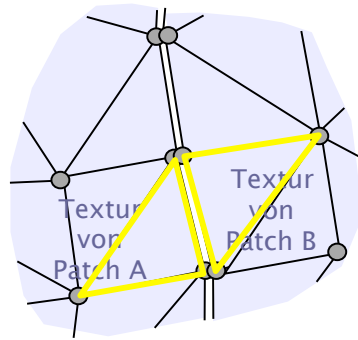
- Example cube map for a [sky box](#):



Texture Atlas vs. Cube Map

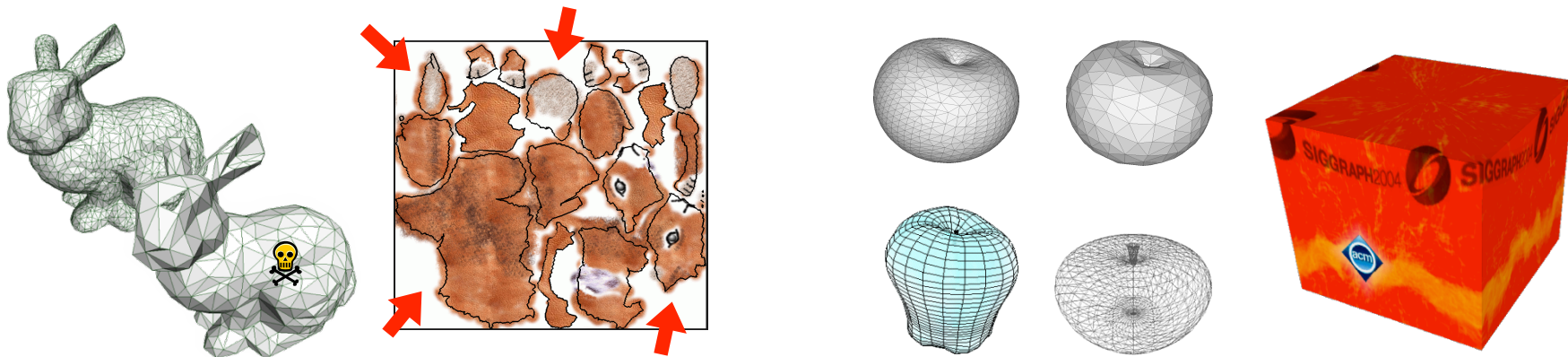


Texture Atlas vs. Cube Map



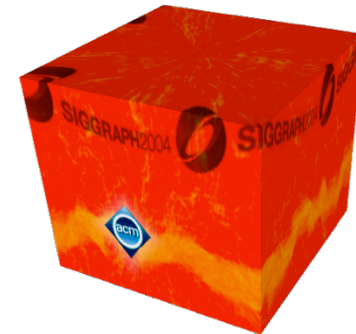
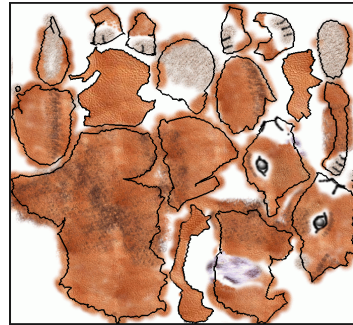
- Must prevent seams manually
 - E.g., by making colors match across seams
- MIP-mapping is difficult

- No seams automatically
 - There are no gaps in the parameter domain
- MIP-mapping is okay



- Must prevent seams manually
- Triangles may lie within the patches
- MIP-mapping is difficult
- Only valid for a specific mesh
- Texels are wasted

- No seams automatically
- Triangles can lie in multiple patches
- MIP-mapping is okay
- Valid for many meshes
- All texels are used



- Must prevent seams manually
- Triangles may lie in the plane of the patches
- MIP-mapping is difficult
- Only valid for a specific mesh
- Textures are wasted

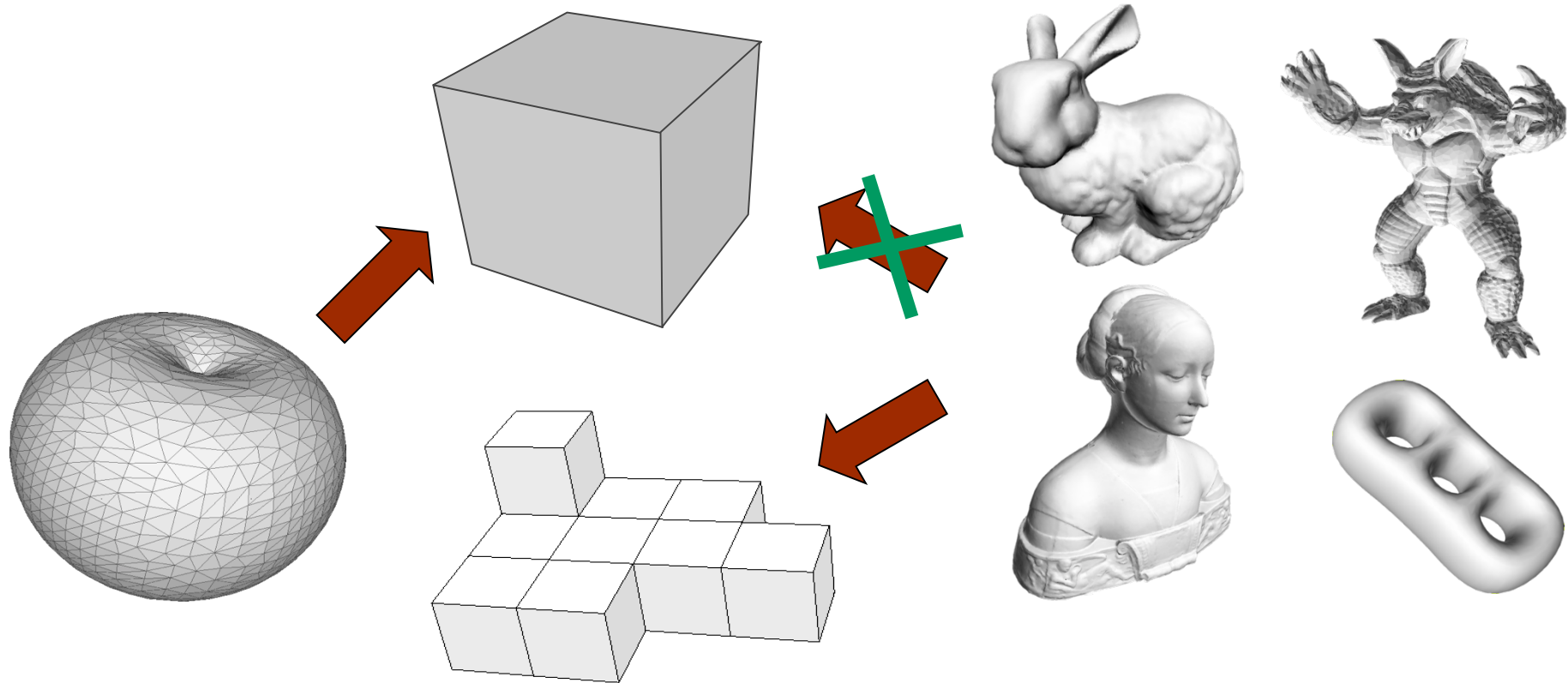
Works for any mesh

- No seams automatically
- Triangles can lie in the plane of the patches
- MIP-mapping is automatic
- Valid for any mesh
- A texture is not wasted

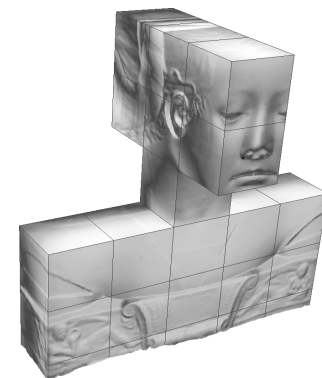
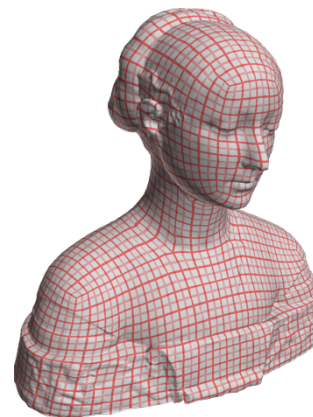
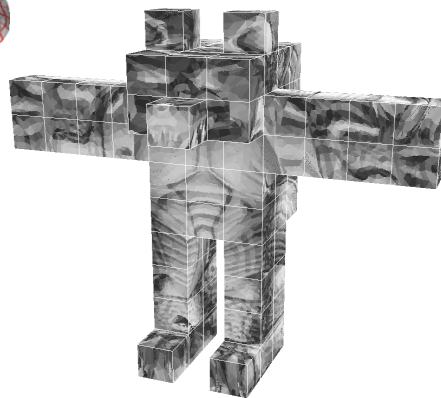
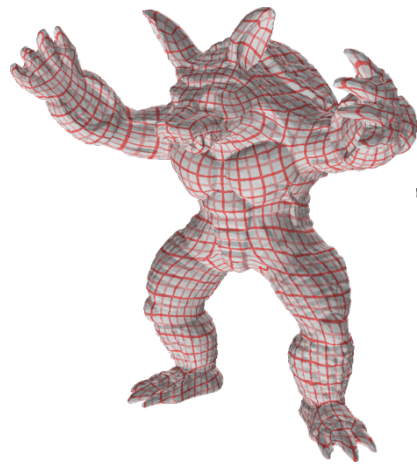
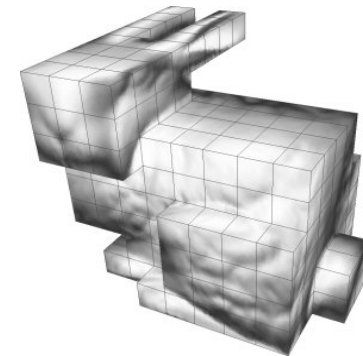
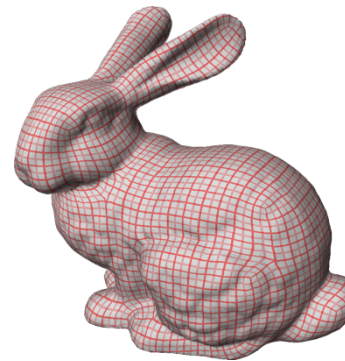
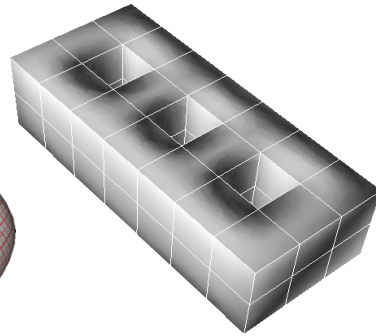
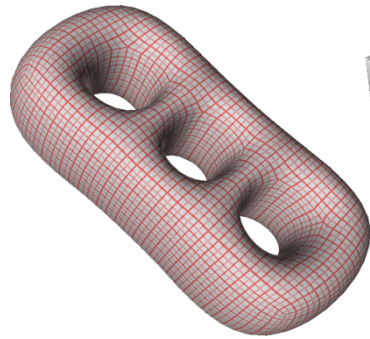
Only for "spheres-like" objects

Polycube Maps

- Use **many** cube maps instead of an individual cube → polycube map
- Adapted to geometry and topology

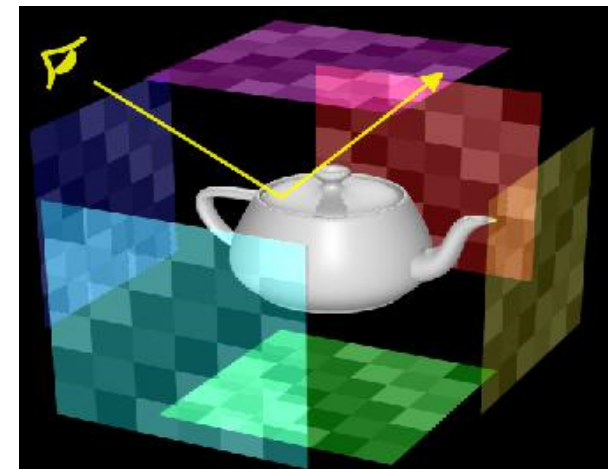


Examples

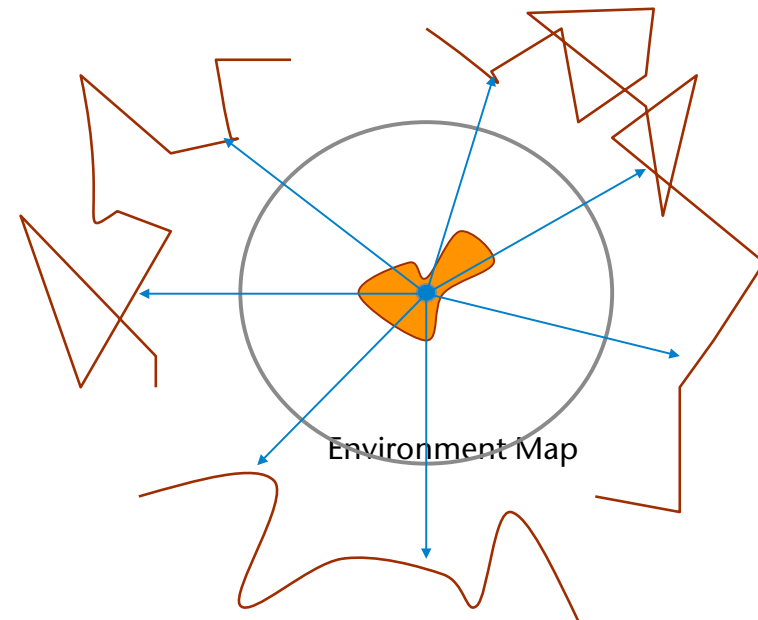


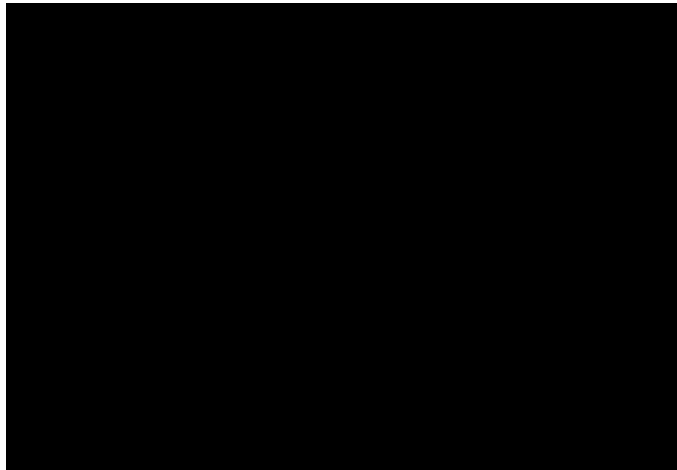
Environment Mapping

- With very reflective objects, one would like to see the surrounding environment reflected in the object
- Ray-tracing can do this, but not the polygonal rendering by rasterization
- The idea of **environment mapping**:
 - "Photograph" the environment in a texture
 - Save this in a so-called **environment map**
 - Use the reflection vector (from the ray) as an index in the texture
 - A.k.a. **reflection mapping**



- For every spatial direction, the environment map saves the color of the light that reaches a specific point
- Only correct for *one* position
- No longer correct if the environment changes





Lance Williams, Siggraph 1985



Flight of the Navigator in 1986;
first feature film to use the technique

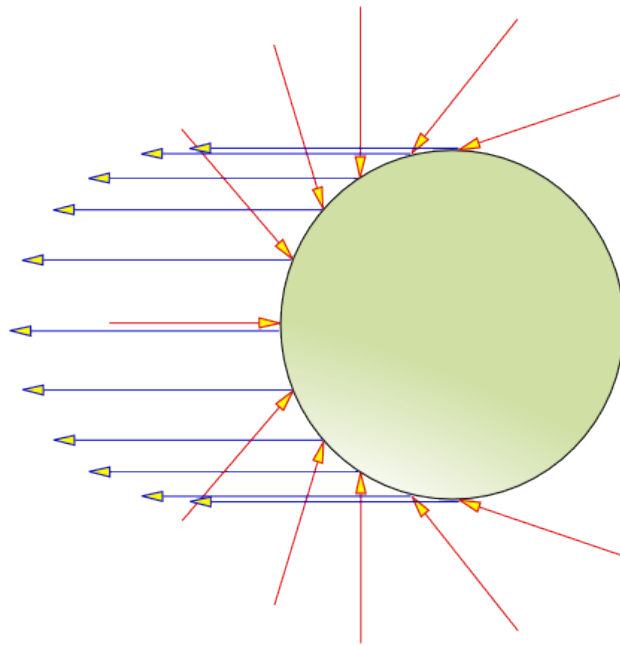


Terminator 2: Judgment Day - 1991
most visible appearance — Industrial Light + Magic

- Generate or load a 2D texture that depicts the environment
- During rasterization, for every pixel of the reflected object...
 1. Calculate the normal \mathbf{n}
 2. Calculate a reflection vector \mathbf{r} from \mathbf{n} and the view vector \mathbf{v}
 3. Calculate **texture coordinates** (u,v) from \mathbf{r}
 4. Color the pixel with the texture value
- The problem: how does one **parameterize** the space of the reflection vectors?
 - I.e.: how does one map spatial directions (= 3D vectors) onto $[0,1] \times [0,1]$?
- Desired characteristics:
 - Uniform sampling (number of texels per solid angle should be "as constant as possible" in all directions)
 - View-independent → only one texture for all camera positions
 - Hardware support (texture coordinates should be easy to generate)

Spherical Environment Mapping

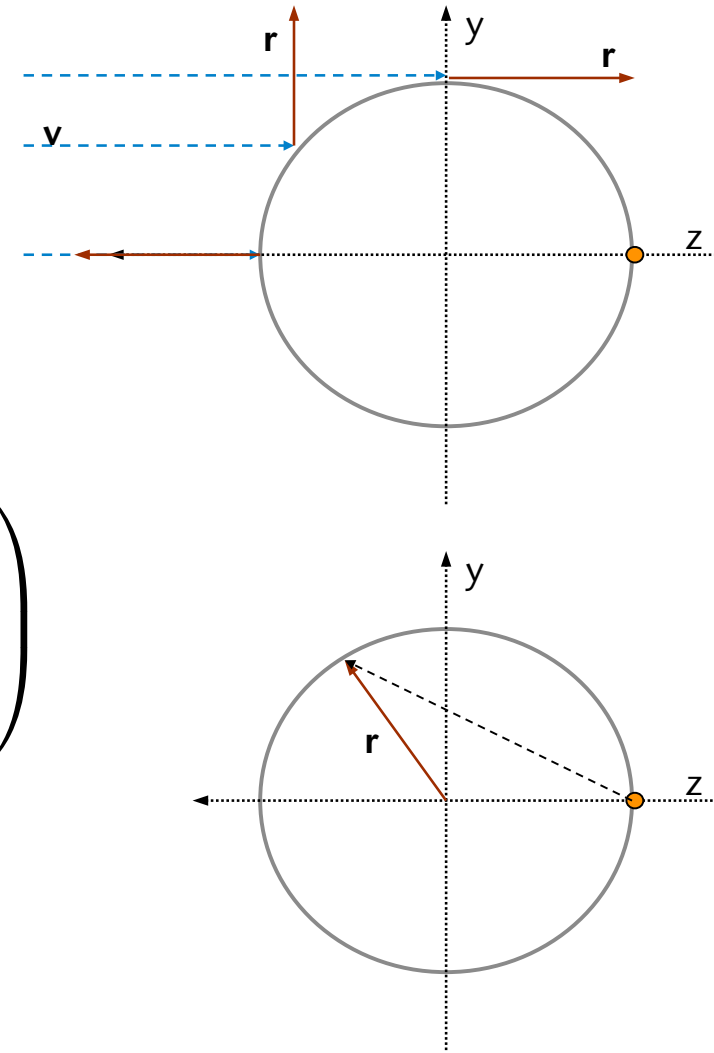
- Generating the environment map (= texture):
 - Photography of a reflective sphere; or
 - Ray-tracing of the scene with all primary rays being reflected at a perfectly reflective sphere



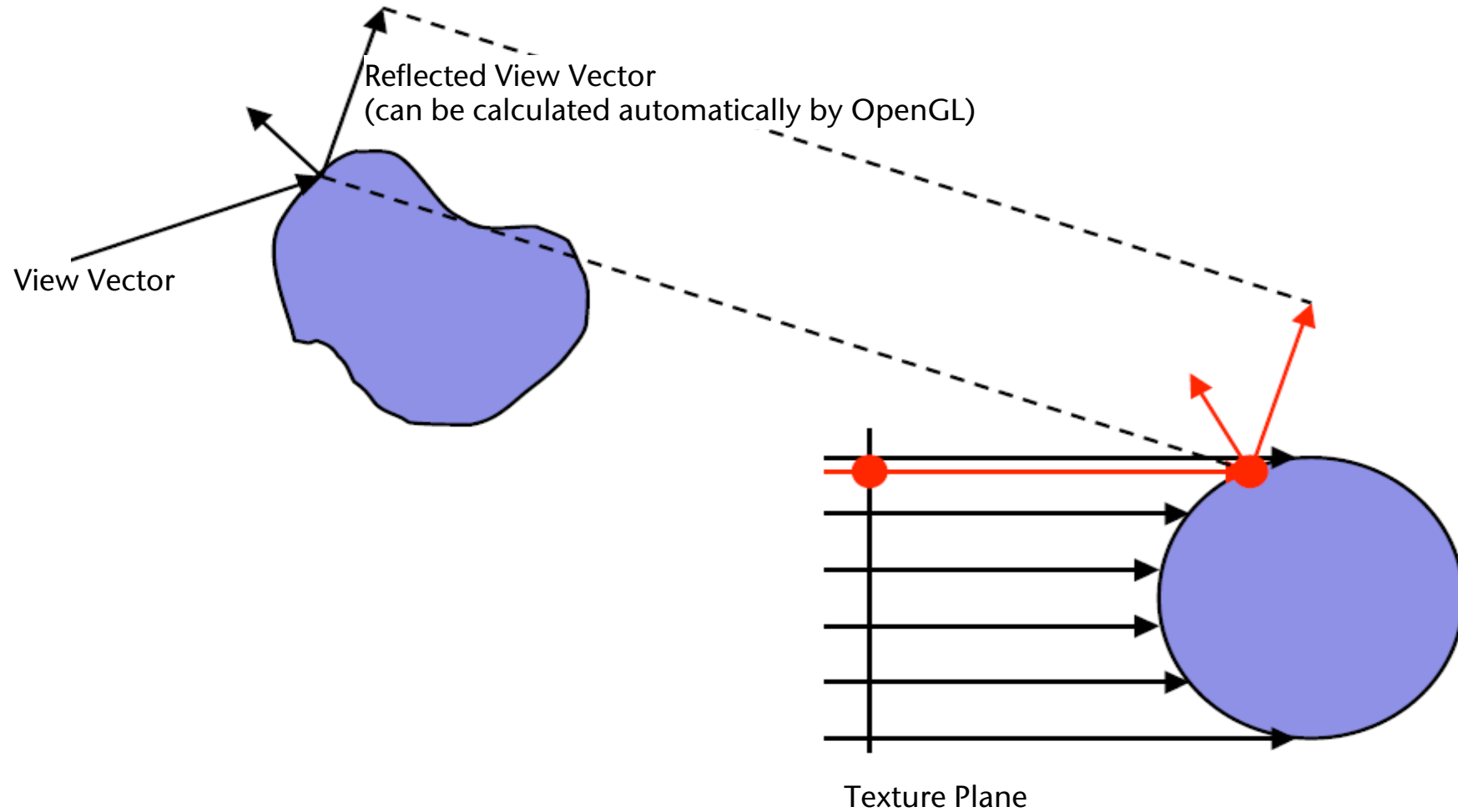
■ Mapping of the directional vector \mathbf{r} onto (u,v) :

- The sphere map contains (theoretically) a color value for **every** direction, except $\mathbf{r} = (0, 0, -1)$
- Mapping:

$$\begin{pmatrix} u \\ v \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \frac{r_x}{\sqrt{r_x^2 + r_y^2 + (r_z + 1)^2}} + 1 \\ \frac{r_y}{\sqrt{r_x^2 + r_y^2 + (r_z + 1)^2}} + 1 \end{pmatrix}$$



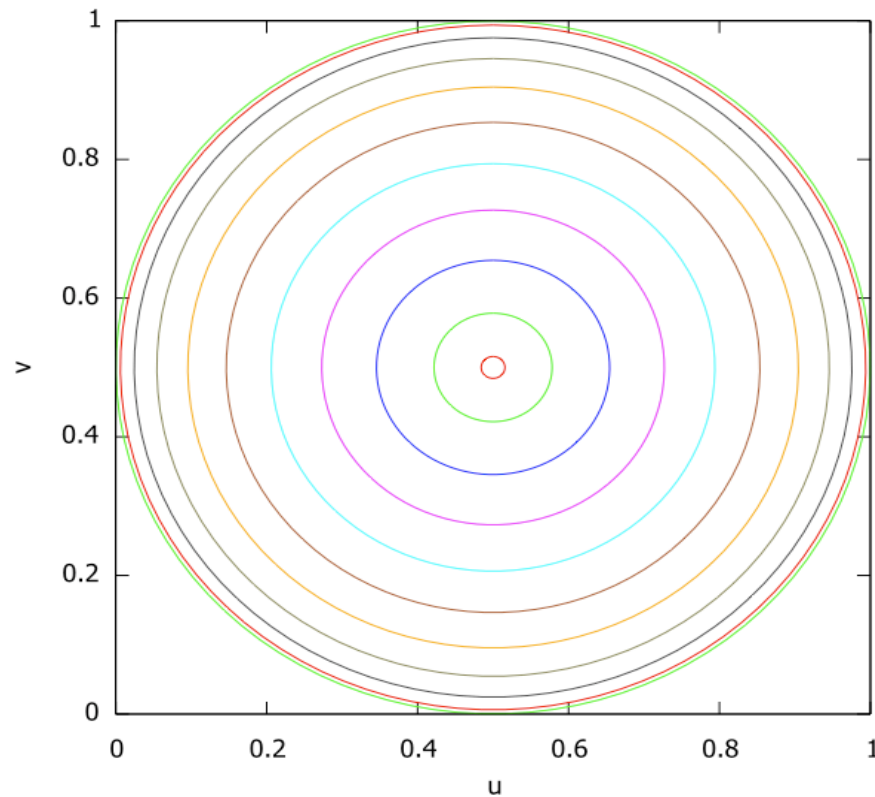
- Application of the sphere mapping to texturing:



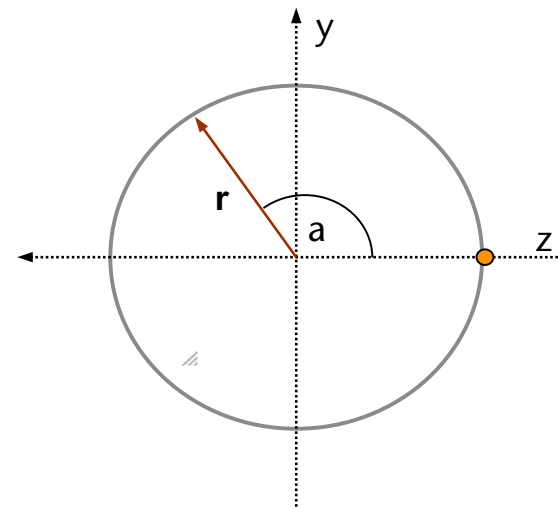
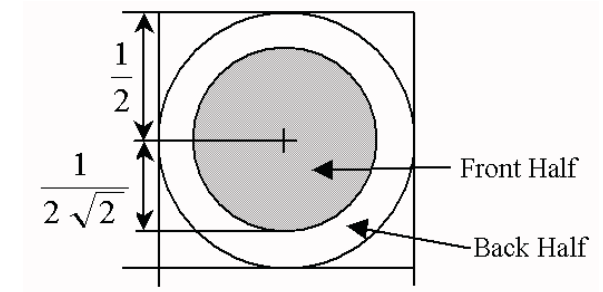
Simple Example



- Unfortunately, the mapping/sampling is not very uniform:



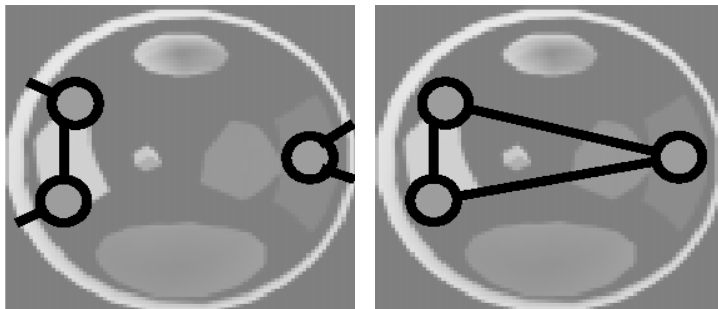
- a = 0.0 pi —
- a = 0.1 pi —
- a = 0.2 pi —
- a = 0.3 pi —
- a = 0.4 pi —
- a = 0.5 pi —
- a = 0.6 pi —
- a = 0.7 pi —
- a = 0.8 pi —
- a = 0.9 pi —
- a = 1.0 pi —



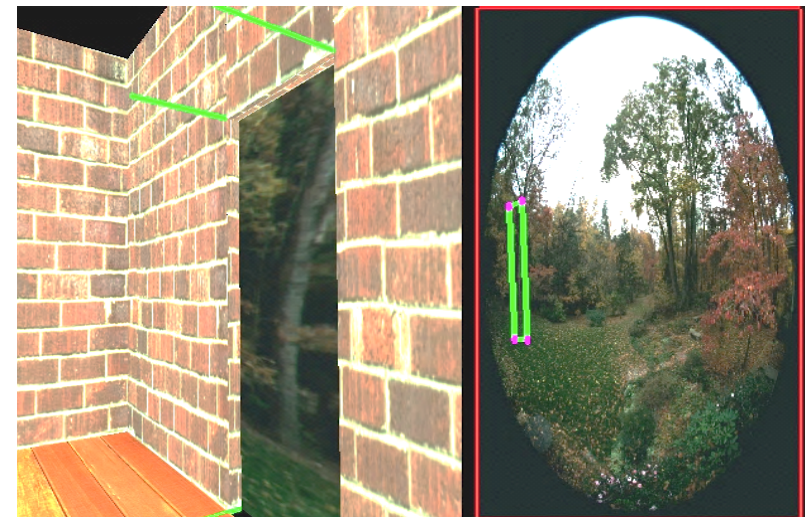
- Texture coords are interpolated incorrectly:
 - Texture coords are interpolated linearly (by the rasterizer), but the sphere map is non-linear
 - Long polygons can cause serious "bends" in the texture
 - Sometimes, incorrect wrap-arounds occur with interpolated texture coords
 - *Sparkles / speckles* if the reflecting vector comes close to the edge of the texture (through aliasing and "wrap-around")



Intended/
correct
wrap
through
the sphere
perimeter



2D texturing hardware doesn't know about sphere maps, it just linearly interpolates texture coords



- Other cons:
 - Textures are difficult to generate by program (other than ray-tracing)
 - *Viewpoint dependent*: the center of the spherical texture map represents the vector that goes directly back to the viewer!
 - Can be made *view independent* with some OpenGL extensions
- Pros:
 - Easy to generate texture coordinates
 - Supported in OpenGL

A Piece of Artwork



Reflective balls in the main street of Adelaide, Australia

Idea:

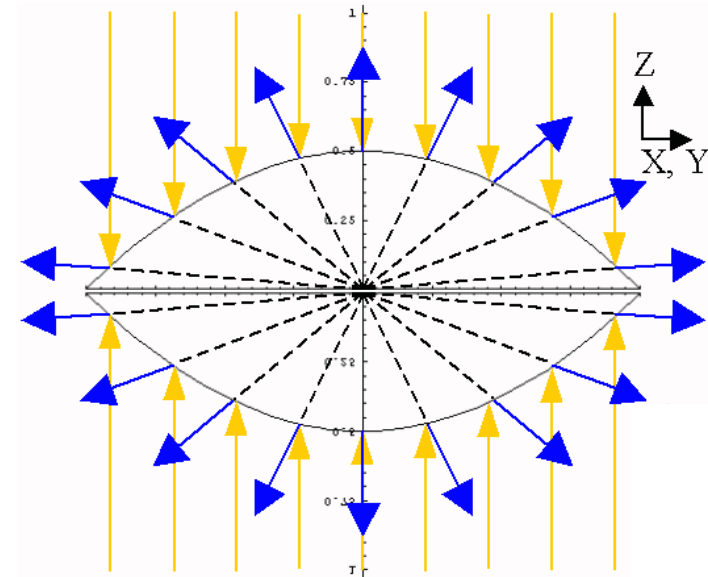
- Map the environment onto **two** textures via a reflective **double paraboloid**

Pros:

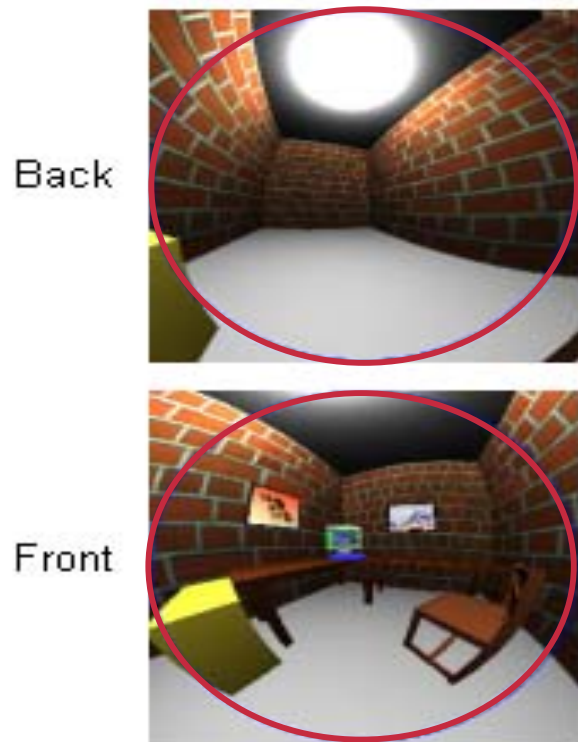
- Relatively uniform sampling
- *View independent*
- Relatively simple computation of texture coordinates
- Also works in OpenGL
- Also works in a single rendering pass (just needs multi-texturing)

Cons:

- Produces artifacts when interpolating across the edge



- Images of the environment (= directional vectors) are still discs (as with the sphere map)
- Comparison:

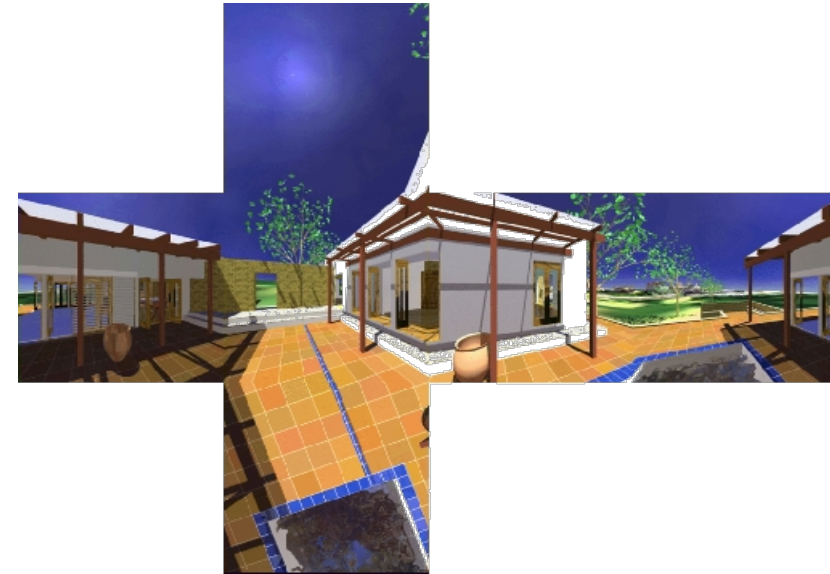


Parabolic environment map

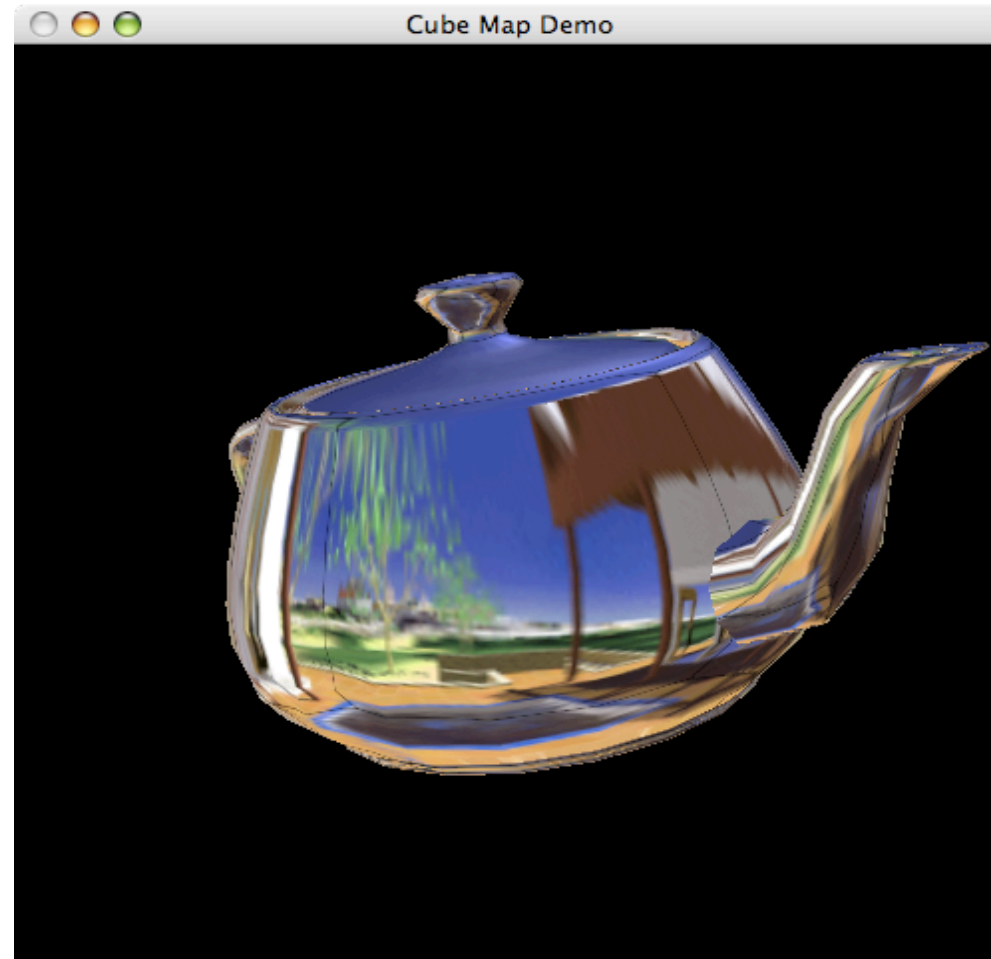


Cubic Environment Mapping

- As before with the "normal" cube maps
- Only difference: use the reflected vector \mathbf{r} for the calculation of the texture coordinates
- This reflected vector can be automatically calculated by OpenGL for each vertex (`GL_REFLECTION_MAP`)



Demo with Static Environment



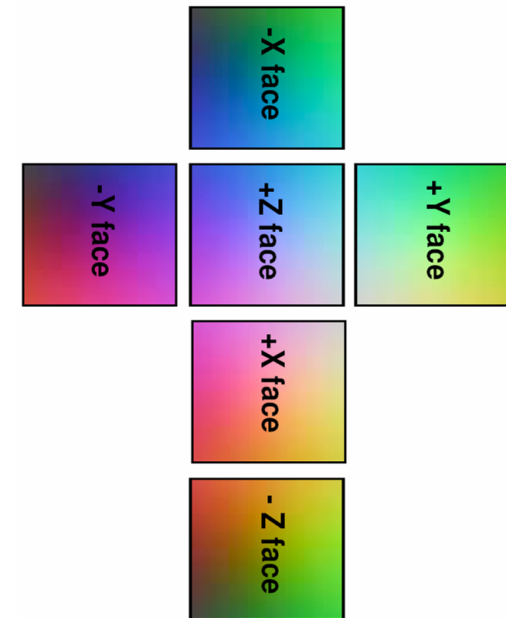
Cube Maps as LUT for Directional Functions

- Further application: one can also use a cube map to store **any** function of **direction!** (as a precomputed lookup table)
- Example: normalization of a vector
 - Every cube map texel (s, t, r) stores this vector

$$\frac{(s, t, r)}{\|(s, t, r)\|}$$

in its RGB channels

- Now one can specify any texture coordinates using `glTexCoord3f()` and receives the normalized vector
- Warning: when using this technique, one should turn off filtering



Dynamic Environment Maps

- Until now: environment map was invalid as soon as something in the environmental scene had changed!
- Idea:
 - Render the scene from the "midpoint" outward (typically 6x for cube map)
 - Transfer framebuffer to texture (using the appropriate mapping)
 - Render the scene again from the viewpoint outward, this time with environment mapping
- Multi-pass rendering
 - Typically used with cube env maps

Dynamic Environment Mapping in OpenGL Using Cube Maps

```

GLuint cm_size = 512;    // texture resolution of each face
GLfloat cm_dir[6][3];   // direction vectors
float dir[6][3] = {
    1.0, 0.0, 0.0,      // right
   -1.0, 0.0, 0.0,      // left
    0.0, 0.0, -1.0,     // bottom
    0.0, 0.0, 1.0,     // top
    0.0, 1.0, 0.0,     // back
    0.0, -1.0, 0.0     // front
};

GLfloat cm_up[6][3] =   // up vectors
{
    0.0, -1.0, 0.0,     // +x
    0.0, -1.0, 0.0,     // -x
    0.0, -1.0, 0.0,     // +y
    0.0, -1.0, 0.0,     // -y
    0.0, 0.0, 1.0,     // +z
    0.0, 0.0, -1.0     // -z
};

GLfloat cm_center[3];   // viewpoint / center of gravity
GLenum cm_face[6] = {
    GL_TEXTURE_CUBE_MAP_POSITIVE_X,
    GL_TEXTURE_CUBE_MAP_NEGATIVE_X,
    GL_TEXTURE_CUBE_MAP_NEGATIVE_Z,
    GL_TEXTURE_CUBE_MAP_POSITIVE_Z,
    GL_TEXTURE_CUBE_MAP_POSITIVE_Y,
    GL_TEXTURE_CUBE_MAP_NEGATIVE_Y
};

// define cube map's center cm_center[] = center of object
// (in which scene has to be reflected)
...

```

```
// set up cube map's view directions in correct order
for ( uint i = 0, i < 6; i + )
    for ( uint j = 0, j < 3; j + )
        cm_dir[i][j] = cm_center[j] + dir[i][j];

// render the 6 perspective views (first 6 render passes)
for ( unsigned int i = 0; i < 6; i ++ )
{
    glClear( GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT );
    glViewport( 0, 0, cm_size, cm_size );
    glMatrixMode( GL_PROJECTION );
    glLoadIdentity();
    gluPerspective( 90.0, 1.0, 0.1, ... );
    glMatrixMode( GL_MODELVIEW );
    glLoadIdentity();
    gluLookAt( cm_center[0], cm_center[1], cm_center[2],
              cm_dir[i][0], cm_dir[i][1], cm_dir[i][2],
              cm_up[i][0], cm_up[i][1], cm_up[i][2] );
    // render scene to be reflected
    ...
    // read-back into corresponding texture map
    glCopyTexImage2D( cm_face[i], 0, GL_RGB, 0, 0, cm_size, cm_size, 0 );
}
```

```

// cube map texture parameters init
glTexEnvf( GL_TEXTURE_ENV, GL_TEXTURE_ENV_MODE, GL_MODULATE );
glTexParameterf( GL_TEXTURE_CUBE_MAP, GL_TEXTURE_WRAP_S, GL_CLAMP );
glTexParameterf( GL_TEXTURE_CUBE_MAP, GL_TEXTURE_WRAP_T, GL_CLAMP );
glTexParameterf( GL_TEXTURE_CUBE_MAP, GL_TEXTURE_MAG_FILTER, GL_LINEAR );
glTexParameterf( GL_TEXTURE_CUBE_MAP, GL_TEXTURE_MIN_FILTER, GL_NEAREST);
glTexGeni( GL_S, GL_TEXTURE_GEN_MODE, GL_REFLECTION_MAP );
glTexGeni( GL_T, GL_TEXTURE_GEN_MODE, GL_REFLECTION_MAP );
glTexGeni( GL_R, GL_TEXTURE_GEN_MODE, GL_REFLECTION_MAP );

// enable texture mapping and automatic texture coordinate generation
glEnable( GL_TEXTURE_GEN_S );
glEnable( GL_TEXTURE_GEN_T );
glEnable( GL_TEXTURE_GEN_R );
glEnable( GL_TEXTURE_CUBE_MAP );

// render object in 7th pass ( in which scene has to be reflected )
...

// disable texture mapping and automatic texture coordinate generation
glDisable( GL_TEXTURE_CUBE_MAP );
glDisable( GL_TEXTURE_GEN_S );
glDisable( GL_TEXTURE_GEN_T );
glDisable( GL_TEXTURE_GEN_R );

```

← Berechnet den Reflection Vector in Eye-Koord.

- On the class's homepage:
 - "OpenGL Cube Map Texturing" (Nvidia, 1999)
 - With example code
 - Here several details are explained (e.g. the orientation)
 - "Lighting and Shading Techniques for Interactive Applications" (Tom McReynolds & David Blythe, Siggraph 1999);
 - SIGGRAPH '99 Course: "Advanced Graphics Programming Techniques Using OpenGL" (ist Teil des o.g. Dokumentes)